

S05 Micromechanics of heterogeneous materials

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MODELLING OF PLASTIC DEFORMATION OF METAL CRYSTALS BY A QUASI-EXTREMAL ENERGY PRINCIPLE

Michał Kursa¹, Henryk Petryk¹

¹ Department of Mechanics of Materials, Institute of Fundamental Technological Research, Poland

mkursa@ippt.pan.pl

Solving of rate-independent polycrystal or single crystal plasticity problems is related to non-uniqueness of incremental solutions. The main difficulty in the crystal plasticity problems arises from indefinite and non-symmetric slip-system interaction matrix when a set of active slip-systems at a material point level has to be determined. The solution and the set of active slip-systems can be found using the computational approach based on the incremental energy minimization [1]. In order to find the solution using the incremental energy minimization, the selective symmetrization of the slip-system interaction matrix restricted to active systems has been proposed. However, a generic rate-problem in crystal plasticity is of non-potential type. The question arises how to select a physically meaningful solution among multiple possibilities when the known extremal principles do not apply.

The new concept to predicting the time-independent response of metal crystals is based on the recently proposed quasi-extremal energy principle (QEP) [2]. The quasi-extremal energy principle enables finding the solution to a generally non-potential problem. The main advantage with the respect to the previous computational approach to rate-independent crystal plasticity problems [1] is that the present approach does not require any symmetrization of the slip-system interaction matrix.

The computational algorithm originally developed for step-by-step minimization of the incremental energy supply, under the symmetry restriction imposed on the constitutive law, is now modified in order to solve the QEP problem. The minimization method applied to solve the QEP problem is based on the augmented Lagrangian method and is implemented within the Wolfram Mathematica environment.

The effectiveness of the modified algorithm is demonstrated by examples of the large deformation of a fcc single crystal under simple shear and uniaxial tension. The approach enables step-by-step selection of the current set of active slip-systems. It is shown that a numerically stable solution can be found for which the number of simultaneously active slip systems does not exceed five. The QEP results are compared to those obtained using approach based on the selective symmetrization and also those of conventional rate-dependent framework. Especially with the simulations in a high-symmetry initial orientation, where several equivalent solutions exist, significant differences are visible. Moreover, the numerical simulations have been compared to the available experimental results, showing the benefits of using the computational approach based on QEP.

[1] Petryk H., Kursa, M. Incremental work minimization algorithm for rate-independent plasticity of single crystals. *Int. J. Num. Meth. Engng.* 104: 157-184, 2015.

[2] Petryk H. A quasi-extremal energy principle for non-potential problems in rate-independent plasticity. *J. Mech. Phys. Solids* 136: 103691, 2020.