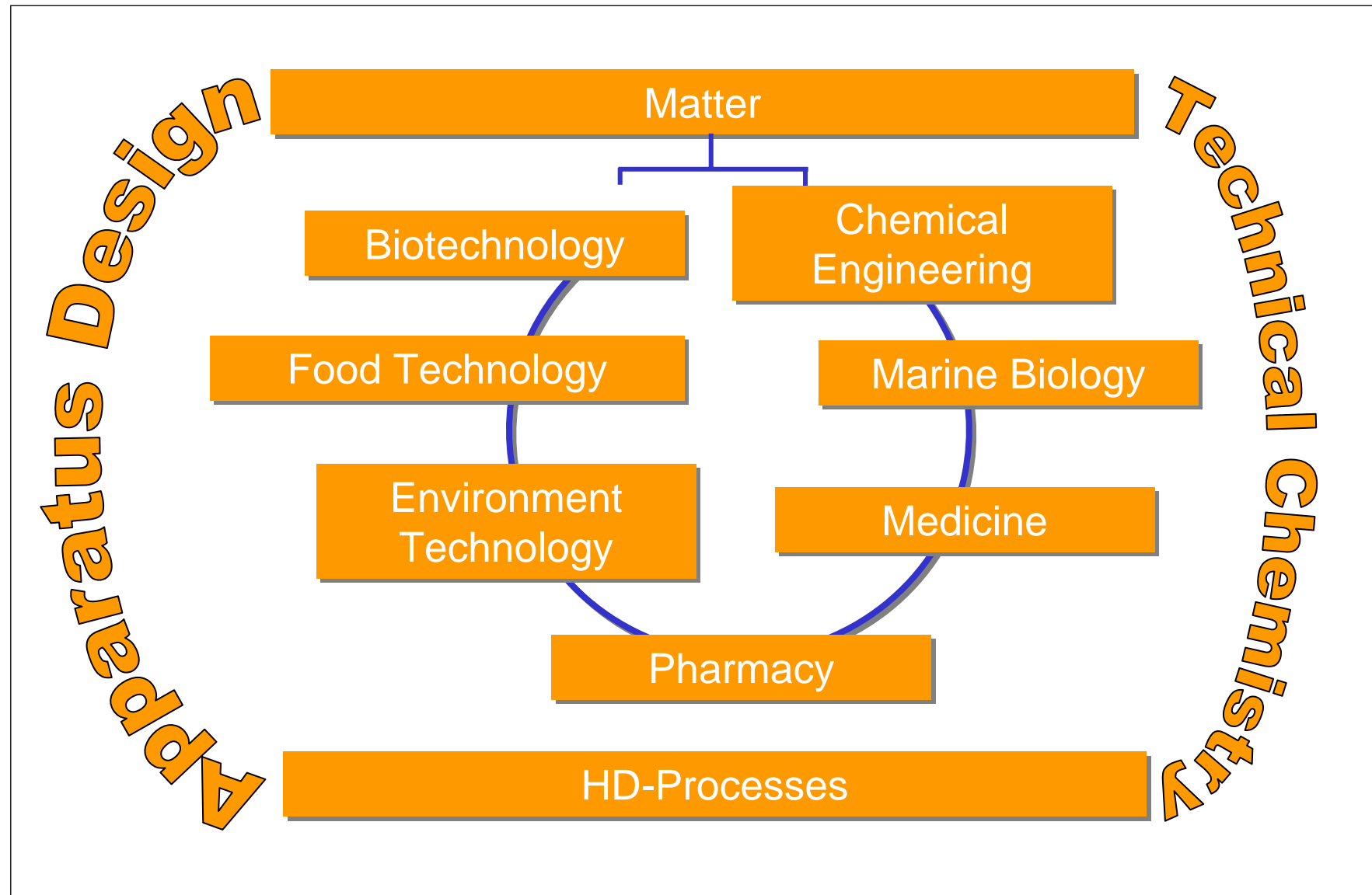
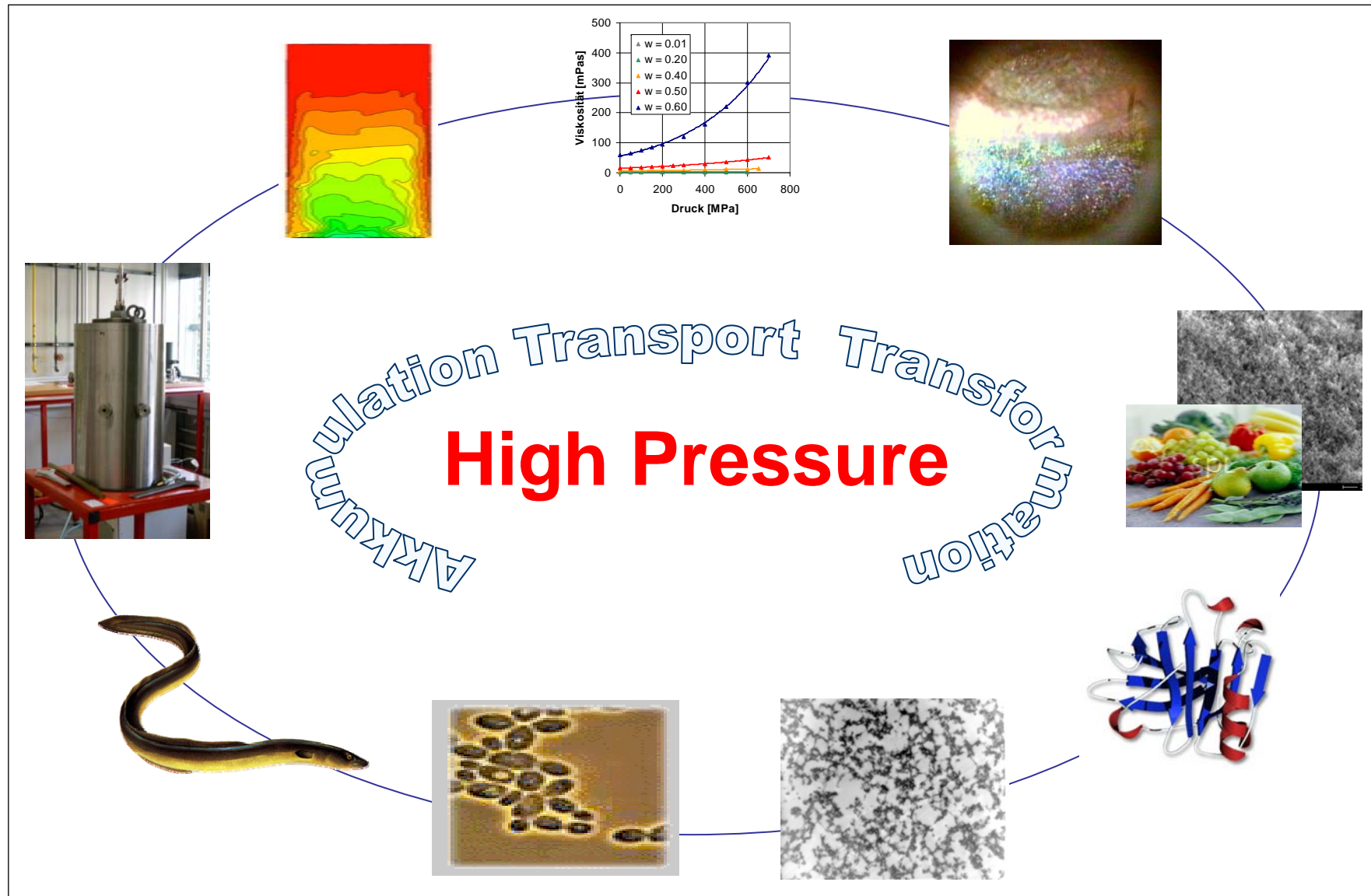


# High Pressure Rheology of Liquid Biomaterials

Albert J. Baars  
Institute of Fluidmechanics (LSTM)  
Friedrich-Alexander-University Erlangen-Nuremberg

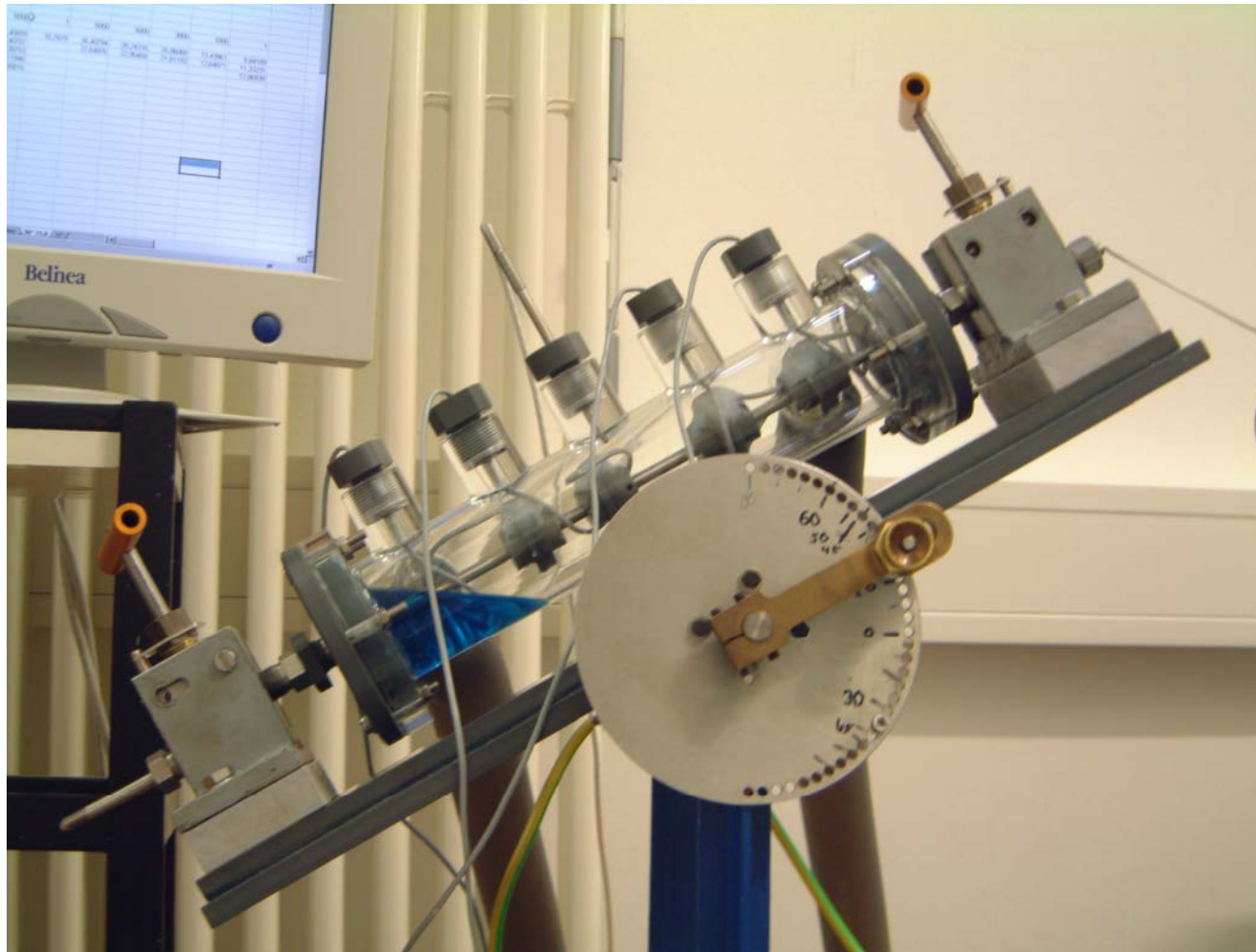
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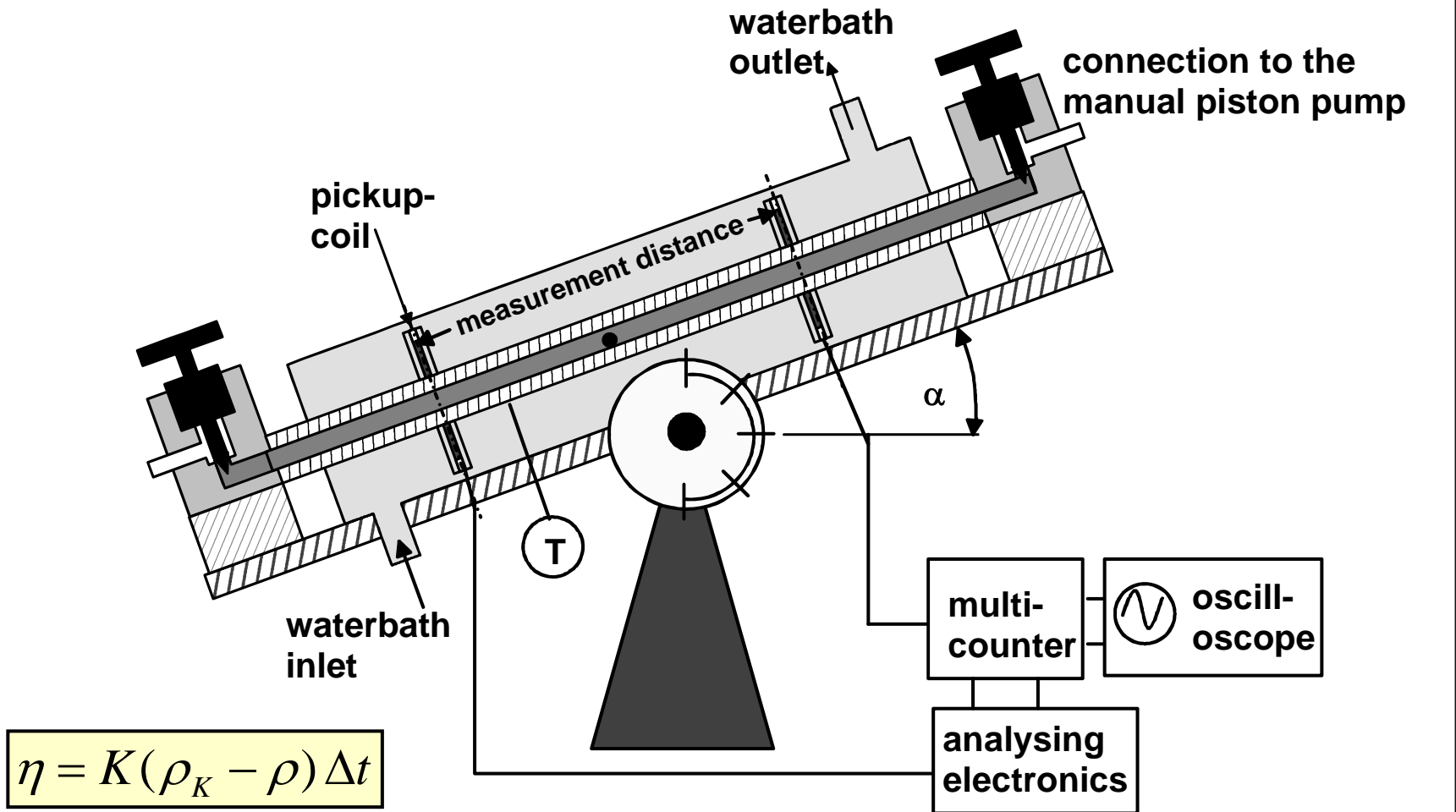
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# Höppler Viscosimeter



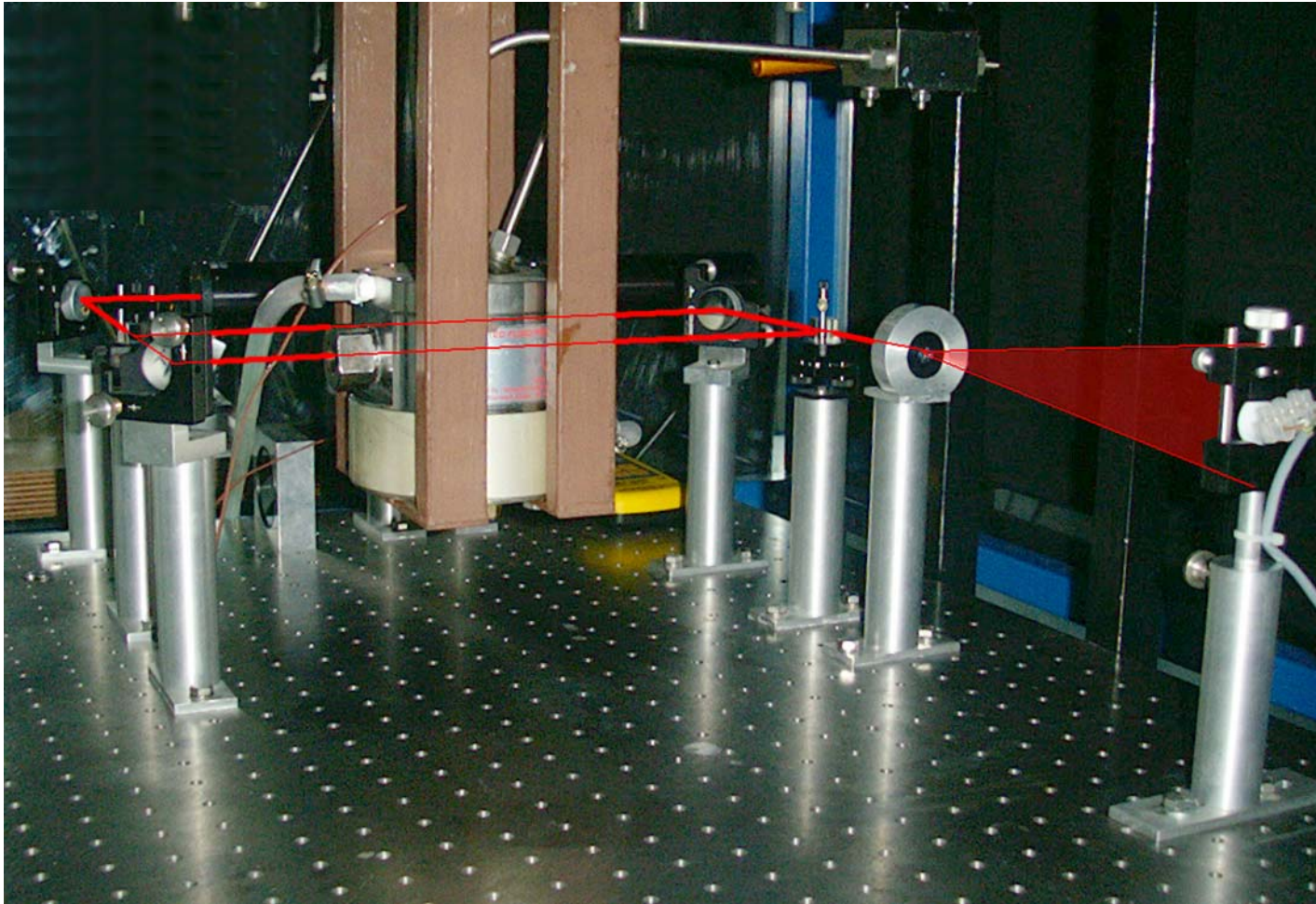
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# Höppler Viscosimeter



Först et al. (2000)

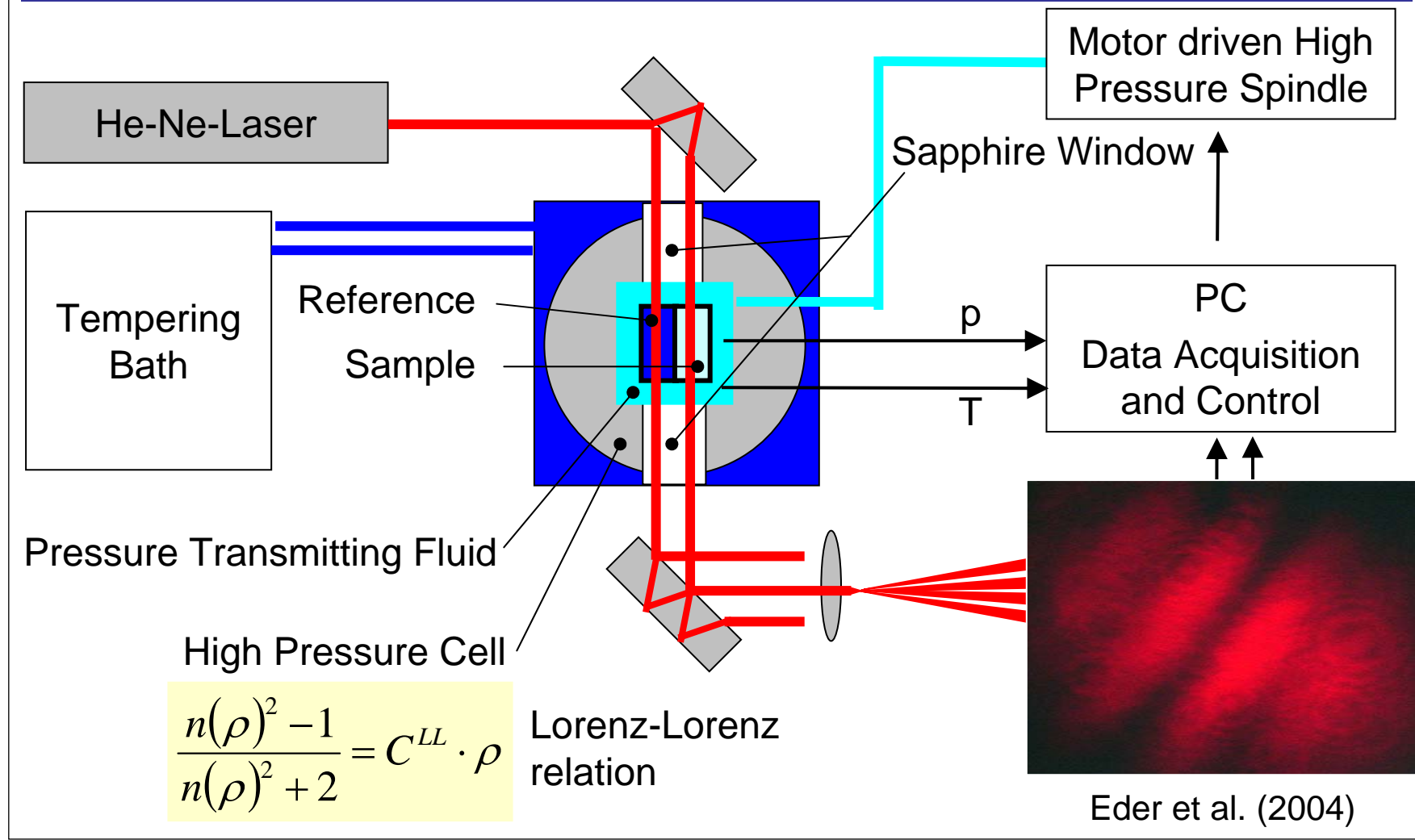
# Jamin Interferometer



Eder et al. (2004)

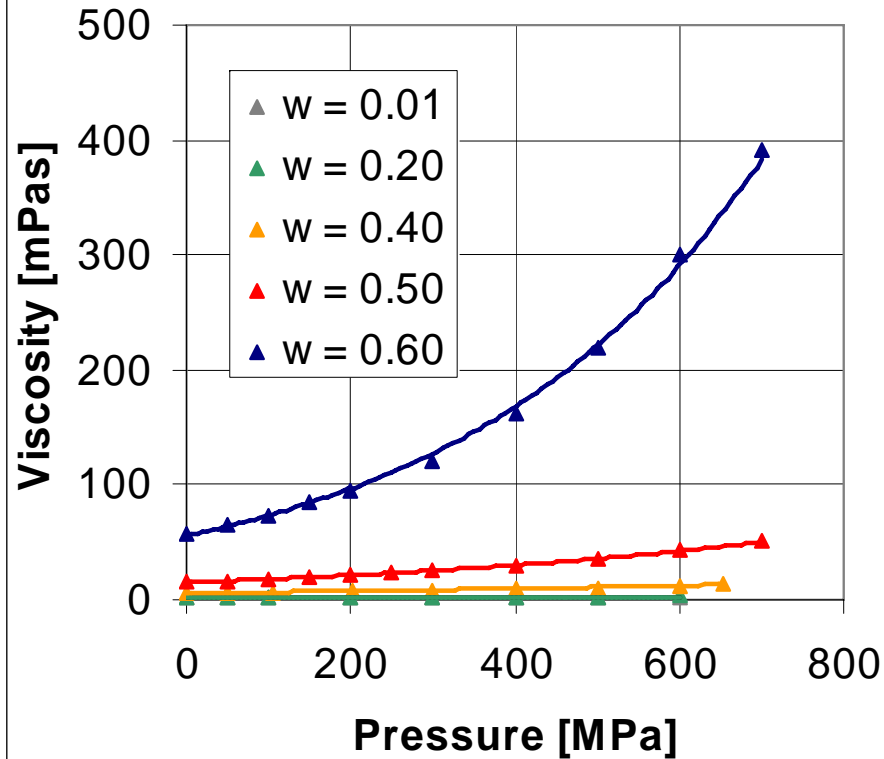
PAN – Warsaw 20.12.2006

# Jamin Interferometer

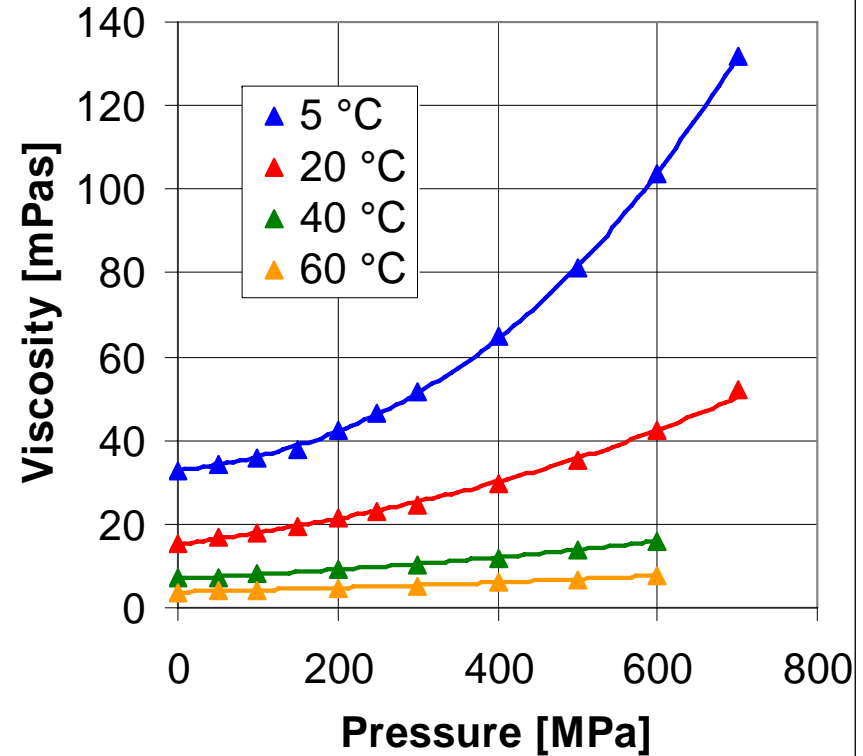


# Viscosity of Aqueous Sucrose Solution

T = 20 °C



w = 0.5



Först et al.



# Viscosity of Aqueous Sucrose Solution

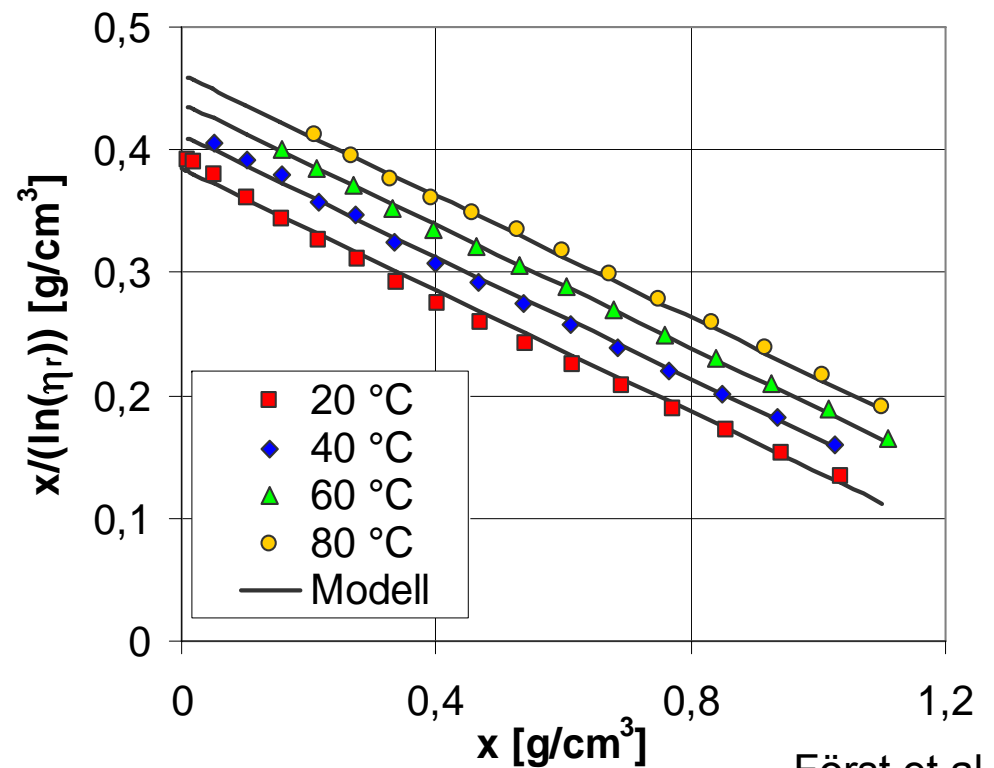
Sucrose Solution – Microscopic Suspension of Rigid Particles (Vand, 1947)

$$\frac{x}{\ln(\eta_r)} = q_0 + q_1 x + \dots$$

$$\eta_r = \frac{\eta(T, p_0)}{\eta_L(T, p_0)}$$

$$x = \rho \cdot w \quad ; \quad q_0 = \frac{\rho_s}{h_0 k_1}$$

$$q_1 = \frac{3(h_0 - 1)}{h_0 k_1 (h_0 + 2)} - \frac{r_2 (k_2 - k_1)}{k_1^2} - \frac{Q}{k_1}$$



Först et al.

# Viscosity of Aqueous Sucrose Solution

Extension of Vands Model

$$\frac{x}{\ln(\eta_r)} = q_0 + q_1 x + \dots$$

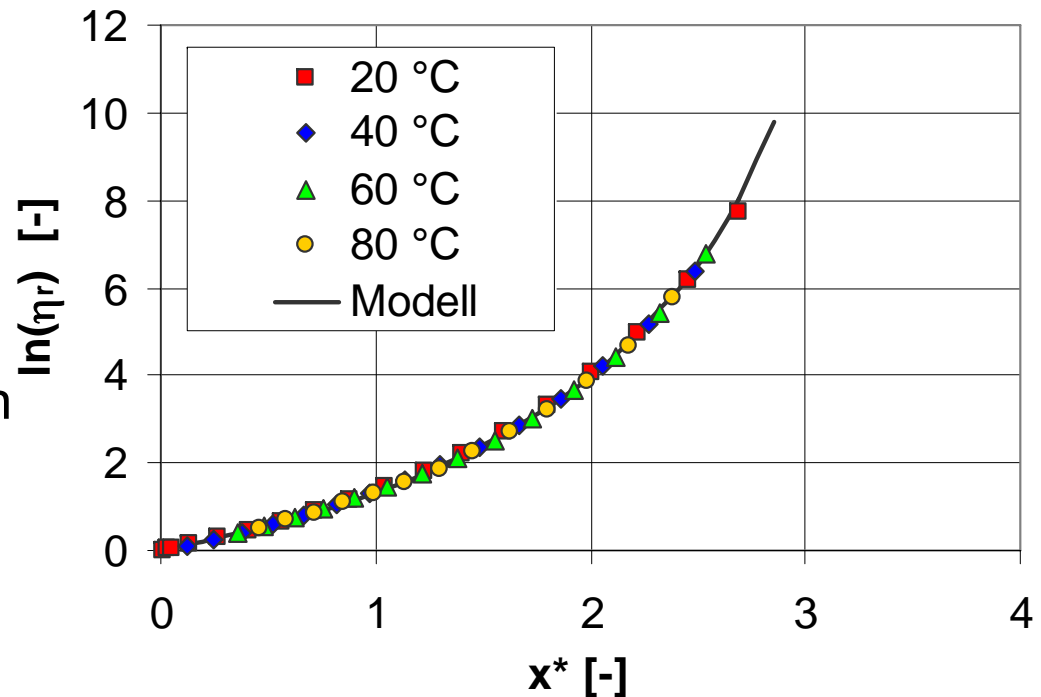
$$\ln \eta_r = \frac{x^*}{1 + q_1 x^*}$$

Relation of Arrhenius

$$q_0 = q_\infty e^{-\frac{E}{RT}}$$

Coordinate Transformation

$$x^* = \frac{x}{q_\infty e^{-\frac{E}{RT}}}$$



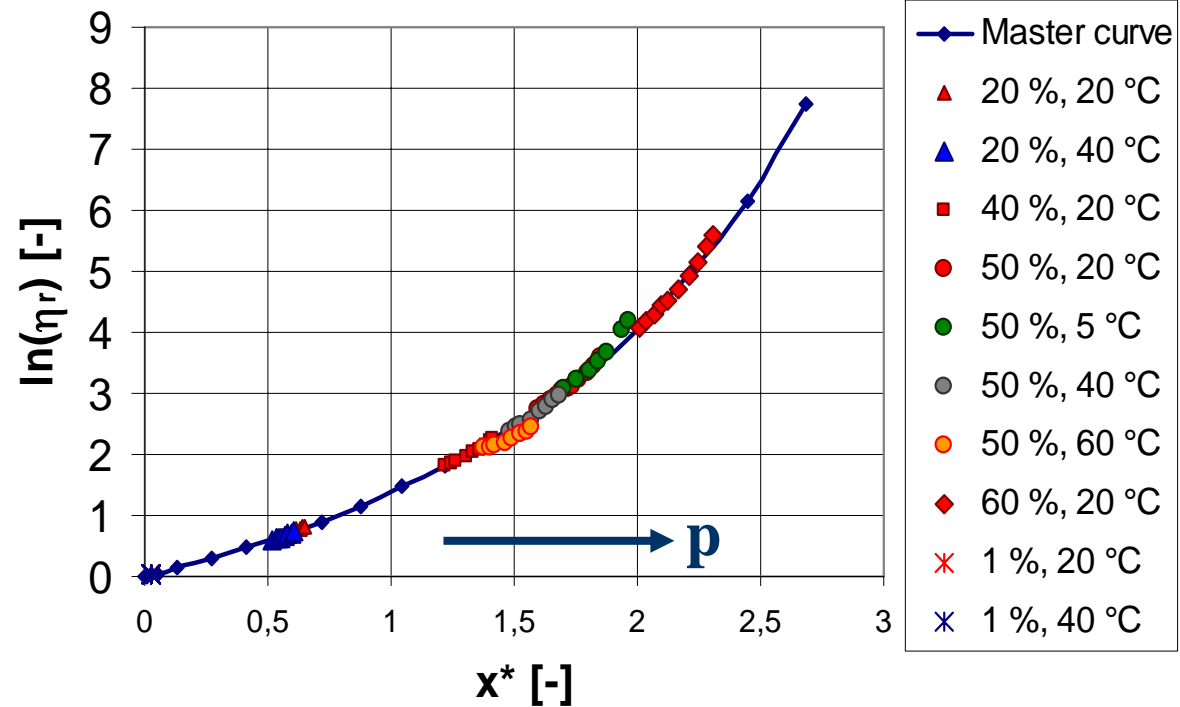
Först et al.

# Viscosity of Aqueous Sucrose Solution

Extension of Vands Model

$$\ln \eta_r = \frac{x^*}{1 + q_1 x^*}$$

$$\eta_r = \frac{\eta(T, p)}{\eta_L(T, p)}$$



Först et al.

# Viscosity of Aqueous $\beta$ -Lg Solution

## Production of the solution

$\beta$ -LG (Sigma-Aldrich, purity 80 %)

solvent: water

mass fraction  $w = 0.01 \dots 0.06$



agitation at 40 °C for 30 min



storing at 4 °C for 12 h

## Experimental procedure

filling



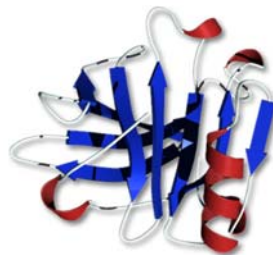
pressure/temperature setting  
(0.1; 50; 100; 140; 180; 220; 260;  
300; 400; 500; 600; 0.1 MPa, 20 °C)



measurement ca. every 2 min

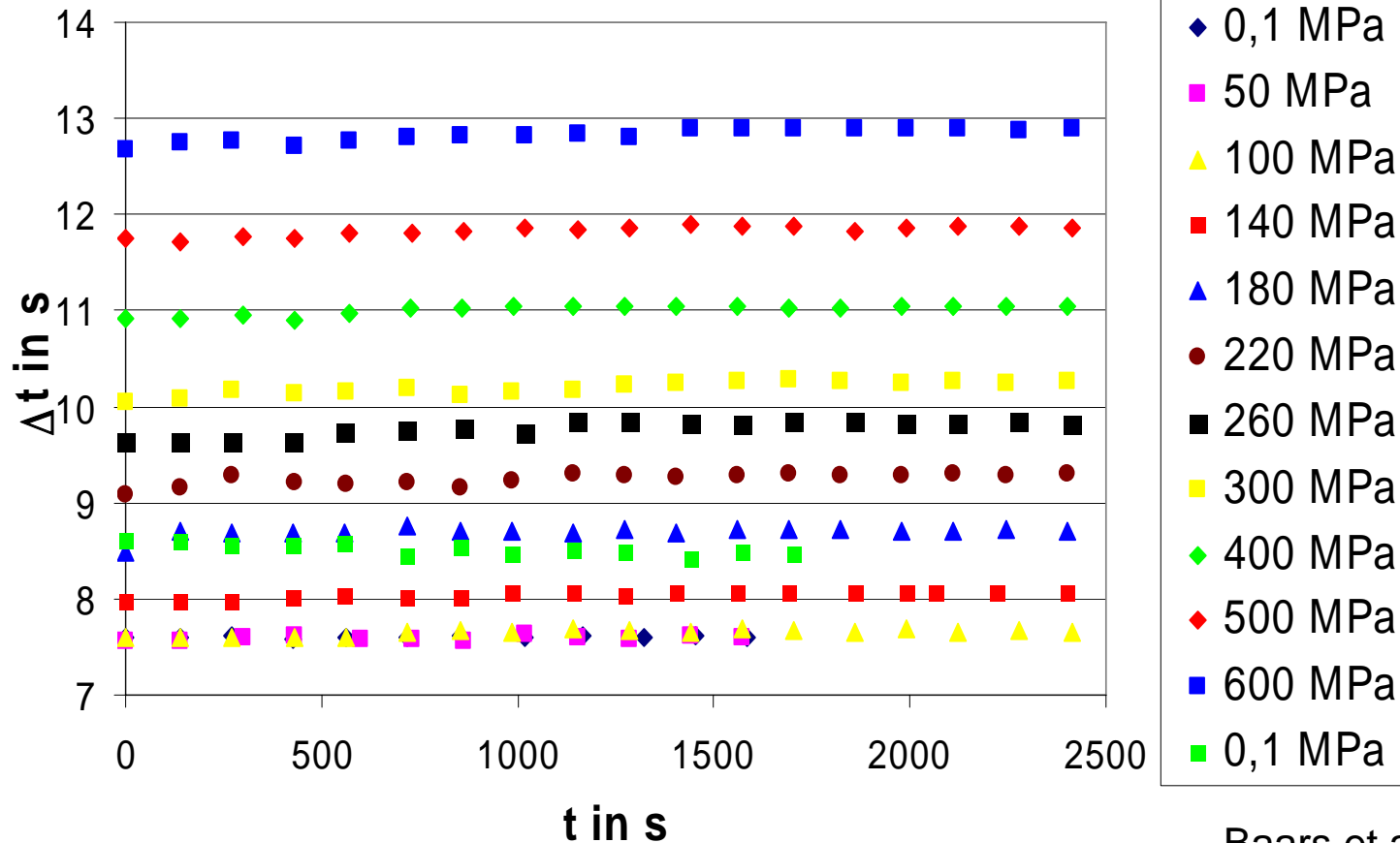


Change of pressure after equilibrium  
and measurement of  $n > 10$  values



# Viscosity of Aqueous $\beta$ -Lg Solution

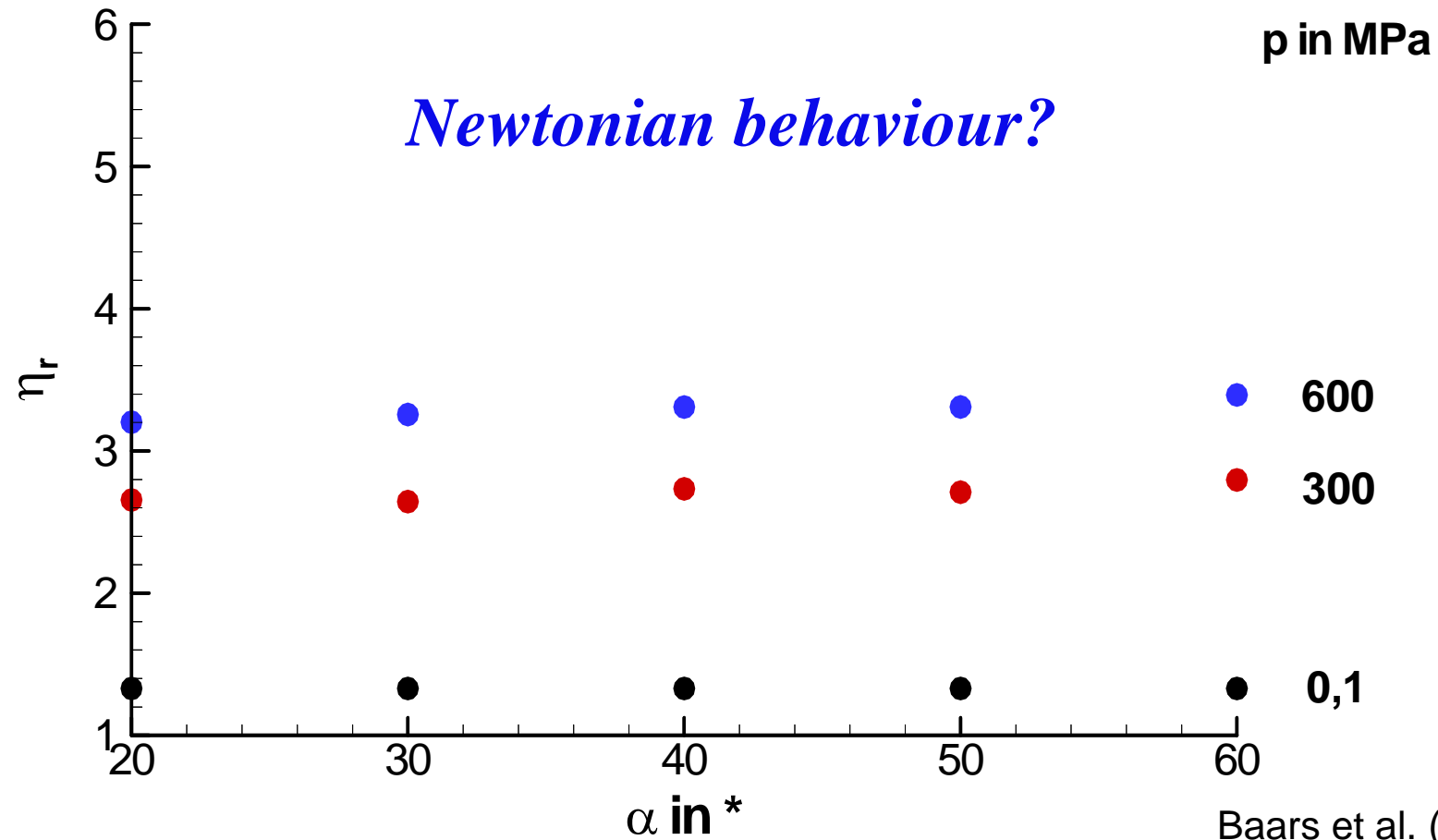
Measured time differences  $\Delta t$  ( $w = 0.04$ )



Baars et al. (2006)

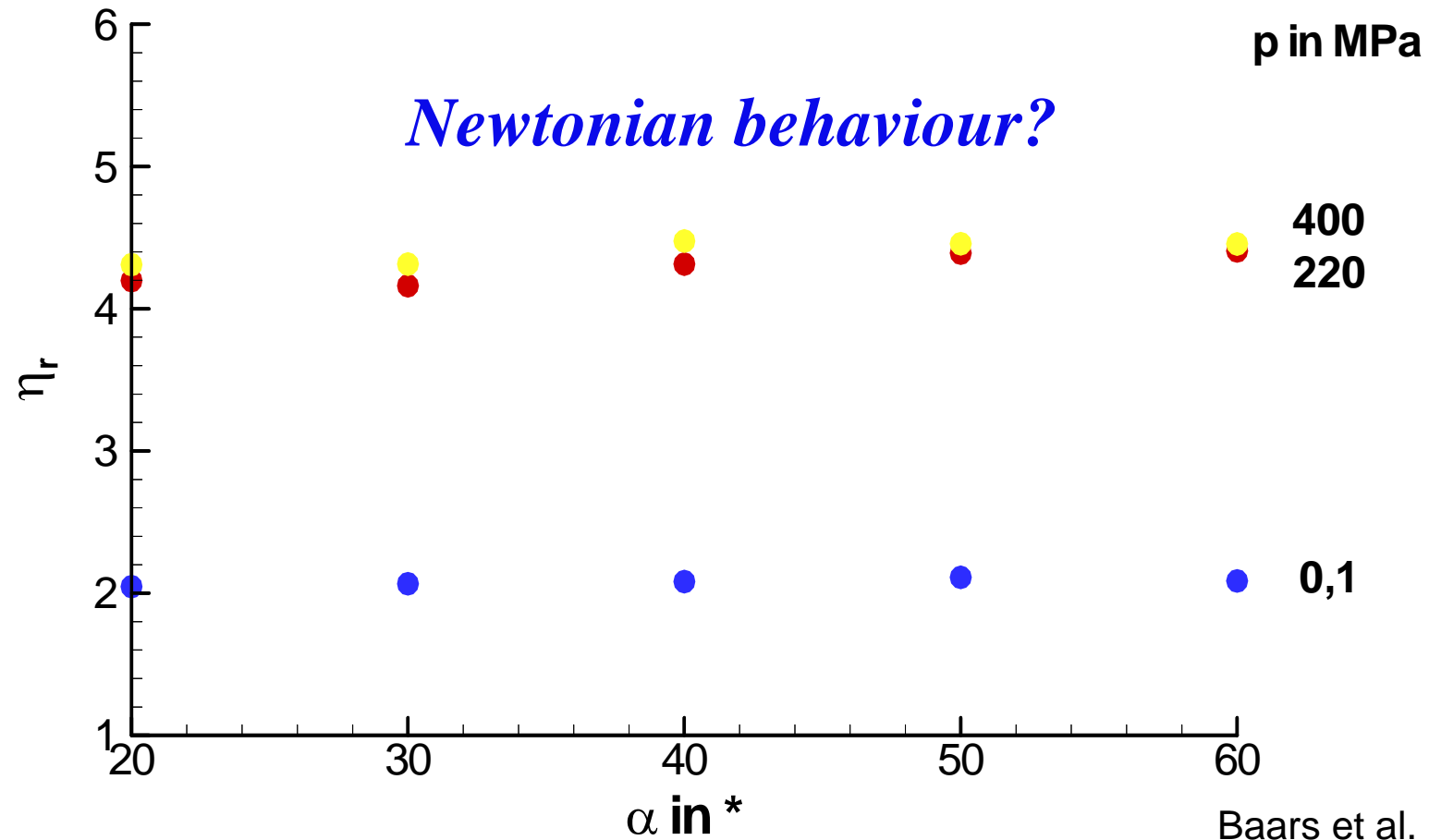
## Viscosity of Aqueous $\beta$ -Lg Solution

$\beta$ -LG solution  $w = 0.06$  (without pre-treatment)



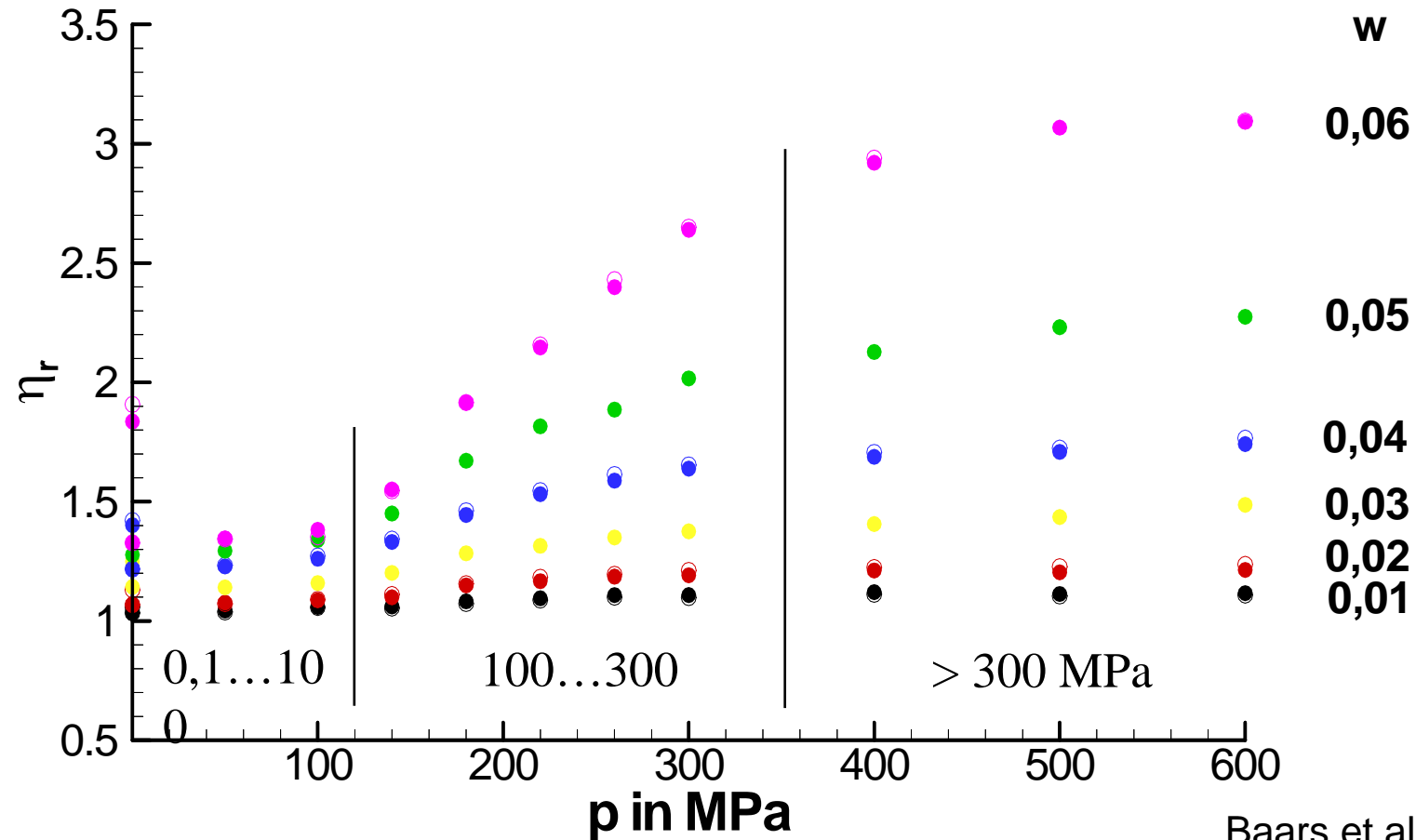
# Viscosity of Aqueous $\beta$ -Lg Solution

$\beta$ -LG solution  $w = 0,06$  (with pre-treatment at 600 MPa)



# Viscosity of Aqueous $\beta$ -Lg Solution

Relative viscosity  $\eta_r$

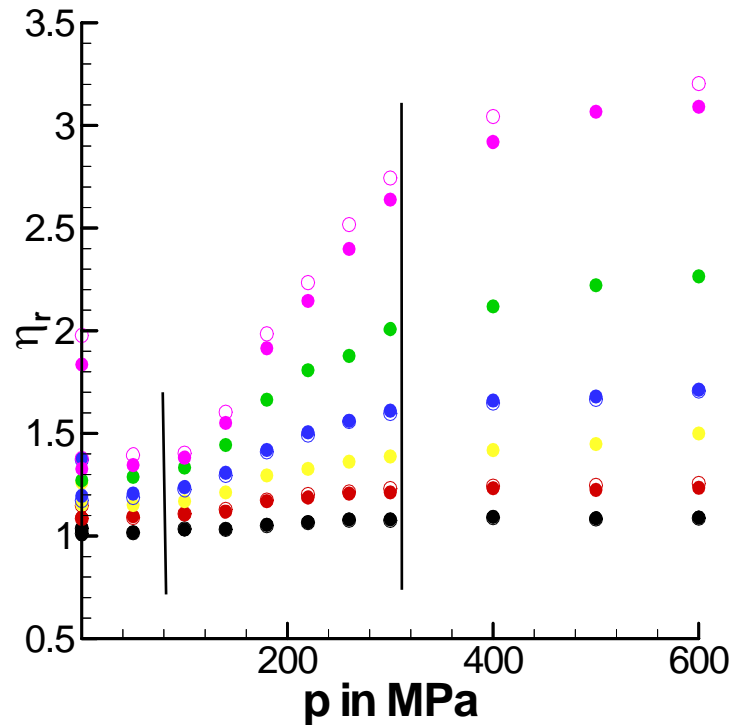


Baars et al. (2006)

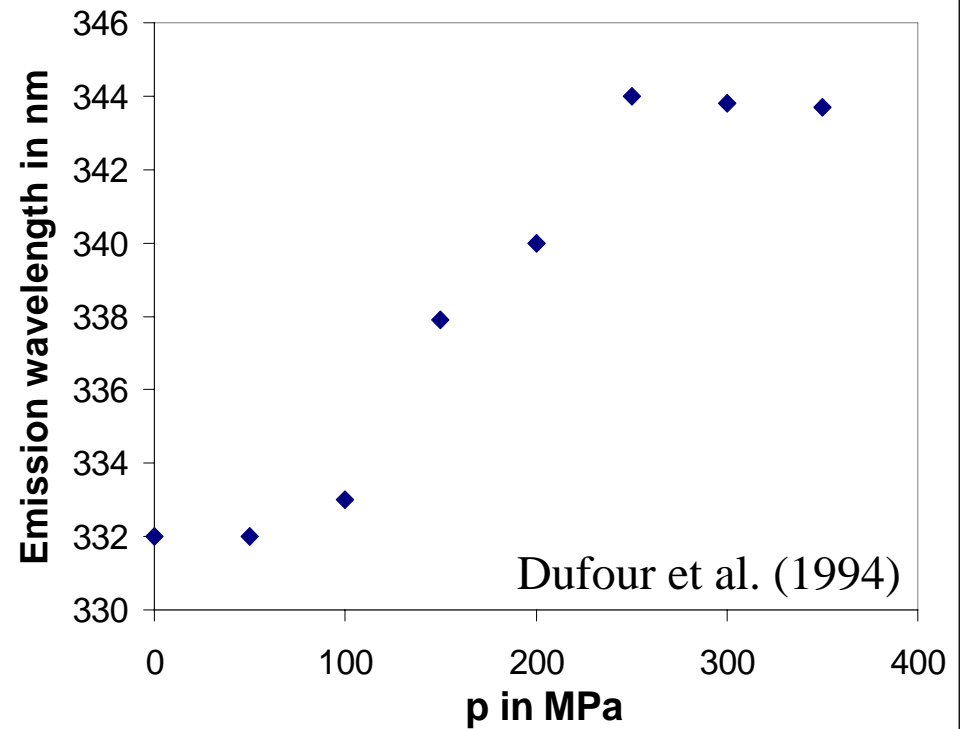


# Viscosity of Aqueous $\beta$ -Lg Solution

## Relative viscosity $\eta_r$



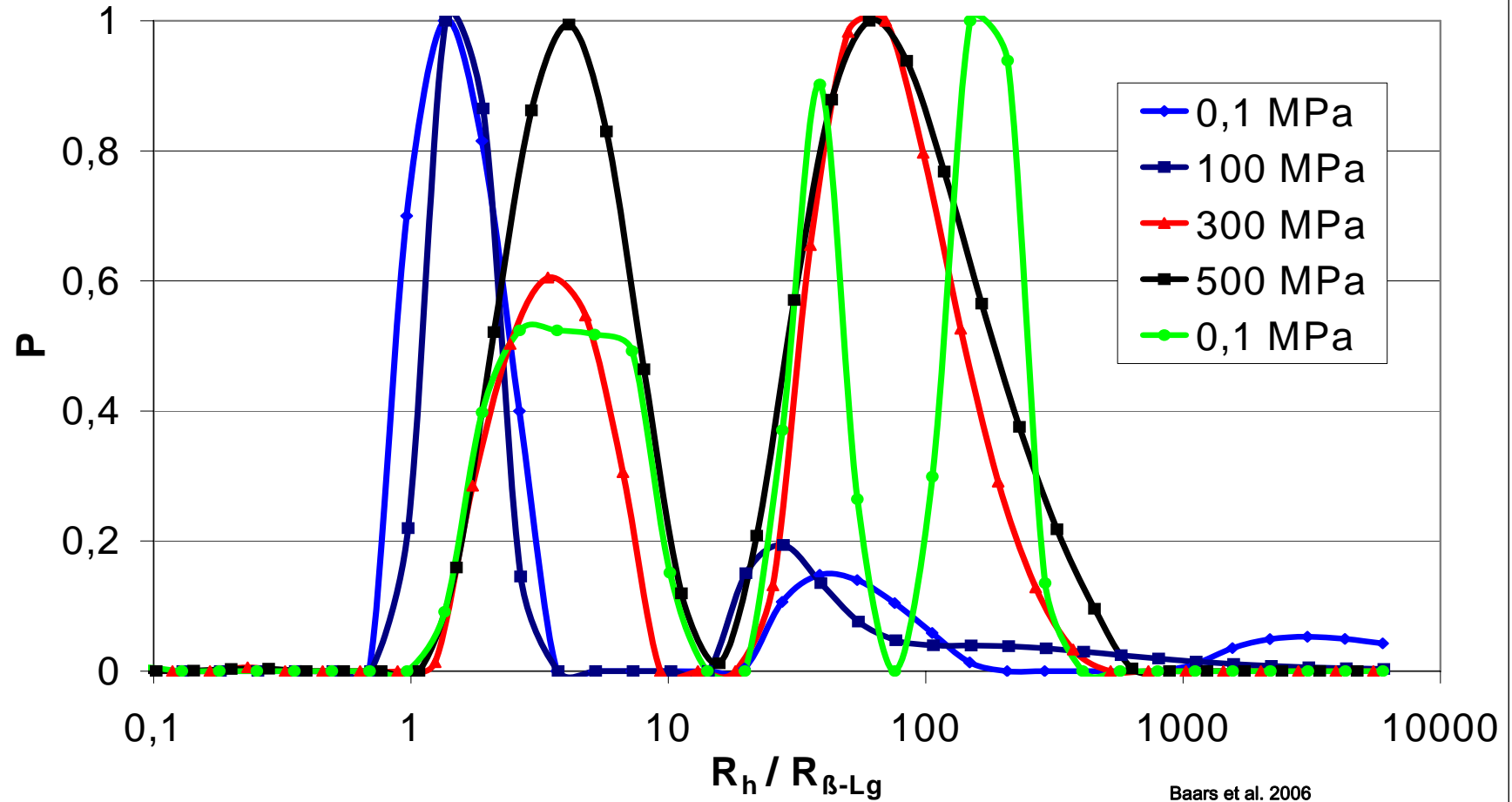
## Fluorescence spectroscopy



Baars et al. (2006)

# Dynamic / Static Light Scattering

Unweighted distribution of hydrodynamic radius ( $w = 0.02$ ;  $20\text{ }^\circ\text{C}$ )



# Molecular dynamic simulation - CHARMM

covalent binding

van der Waals, Coulomb forces

Newton's second law

$$m_i \frac{d^2 \mathbf{R}_i}{dt^2} = \mathbf{F}_i^{res} = - \frac{d}{d \mathbf{R}_i} \sum_k V_i^k$$

Potentials

Hooke

$$V_b = \frac{1}{2} k_b (b - b_0)^2$$

Coulomb

$$V_{el} = \sum_{i,j} \frac{q_i q_j}{4\pi\epsilon_0 \epsilon_{eff} r_{ij}}$$

Lennard-Jones

$$V_{vdW} = \sum_{i,j} 4\epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right]$$

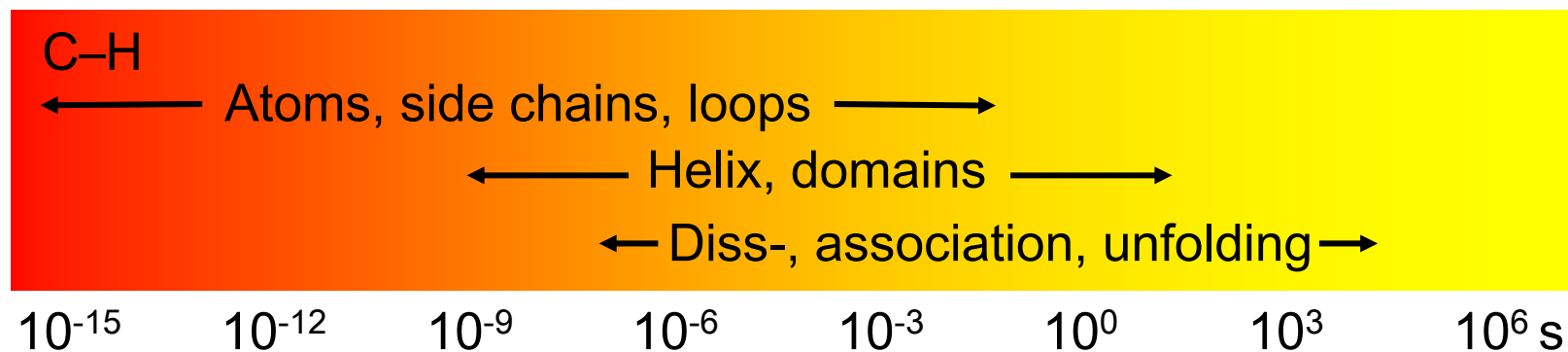
# Molecular dynamic simulation

## Numerical procedure

- Leap Frog - Algorithm

$$\mathbf{a}_i(t) = \frac{\mathbf{F}_i^{res}}{m_i} \quad \rightarrow \quad \begin{aligned} \mathbf{v}_i(t + 0.5\Delta t) &= \mathbf{v}_i(t - 0.5\Delta t) + \mathbf{a}_i(t)\Delta t \\ \mathbf{r}_i(t + \Delta t) &= \mathbf{r}_i(t) + \mathbf{v}_i(t + 0.5\Delta t)\Delta t \end{aligned}$$

- Time step ( $\Delta t$ )

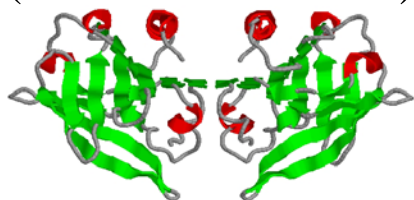


$$\Delta t = \Delta t_{\min} / 10 \quad \rightarrow \quad \Delta t_{\text{C-H}} = 1 \text{ fs}$$

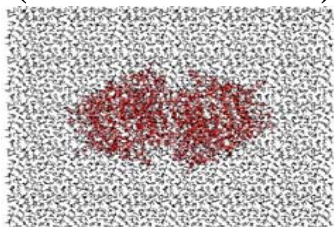
$$\text{SHAKE-BONH-Algorithm} \rightarrow \Delta t_{\text{C-H}} = 2 \text{ fs}$$

# Procedure

Dimer  $\beta$ -Lactoglobulin B  
(RCSB Data Bank)



Solution in water box  
(120x90x90 Å)



$P = 0.1$  MPa,  $T = 298$  K, pH 7  
Equilibration (1 ns)  
Energy minimization

Start

$P = 0.1$  MPa,  $T = 298$  K

$P = P + 50$  MPa (2 ps)

Equilibration (40 ps)  
Energy minimization

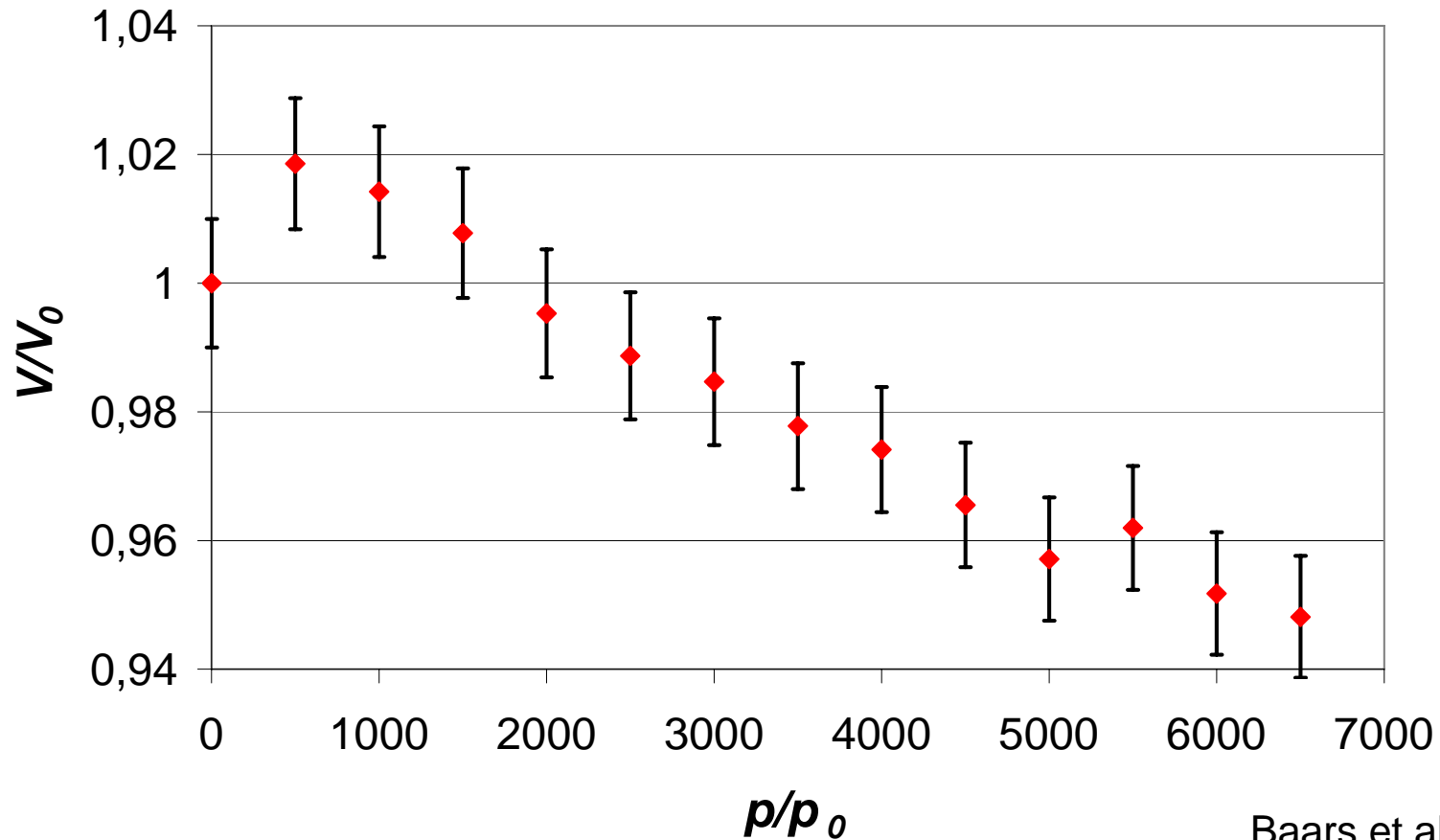
Storage of structure

$P >$   
650 MPa

End

# Results

## Intrinsic volume (Voronoi)



Baars et al. (2006)

## Results

### Isothermal Compressibility (in GPa<sup>-1</sup>)

	<i>Own results</i>		<i>Literature</i>
Total protein	0.110	+/- 0.040	0.14 <sup>a,b</sup>
$\alpha$ -helices	0.087	+/- 0.019	
$\beta$ -Strands	0.115	+/- 0.019	
Loops	0.118	+/- 0.019	
Cavities	0.500	+/- 0.140	0.35-0.69 <sup>b</sup>
Core (-400 MPa)	0.126	+/- 0.030	
Core (450-650 MPa)	0.017	+/- 0.060	

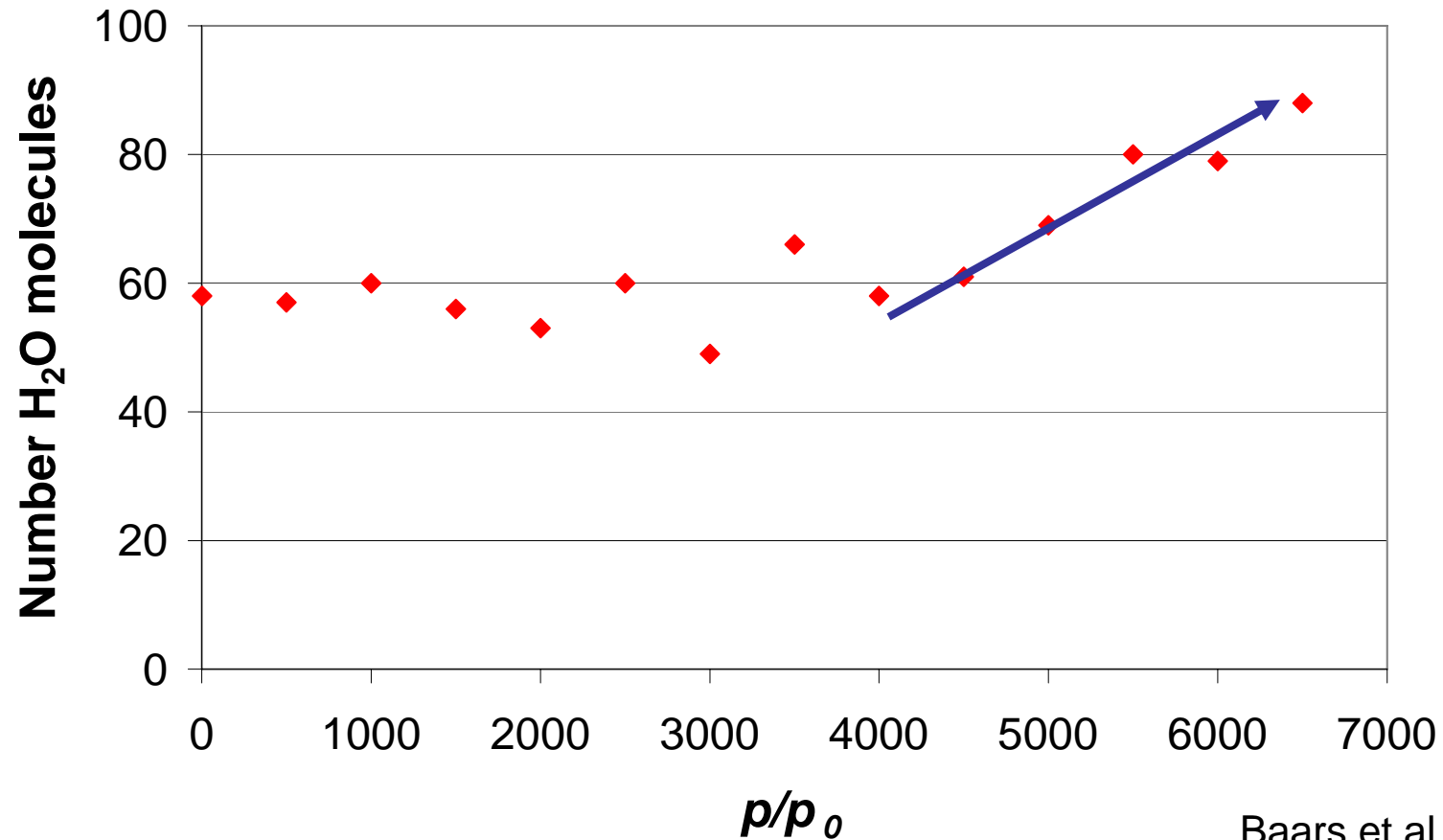
<sup>a</sup> Kharakoz et al. 1993

<sup>b</sup> Mori et al. 2006

Baars et al. (2006)

# Results

Number of H<sub>2</sub>O molecules in the protein

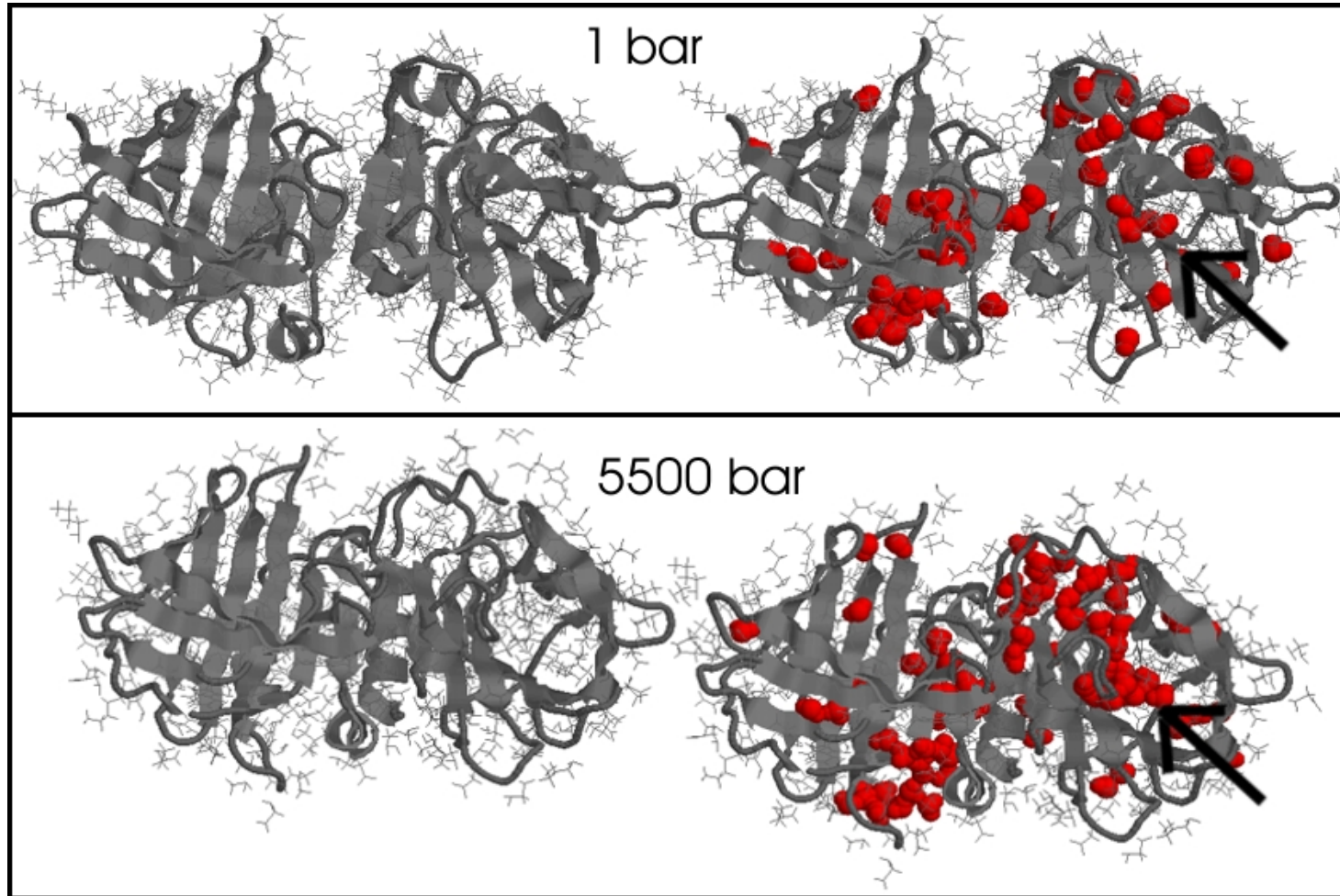


Baars et al. (2006)



# Results

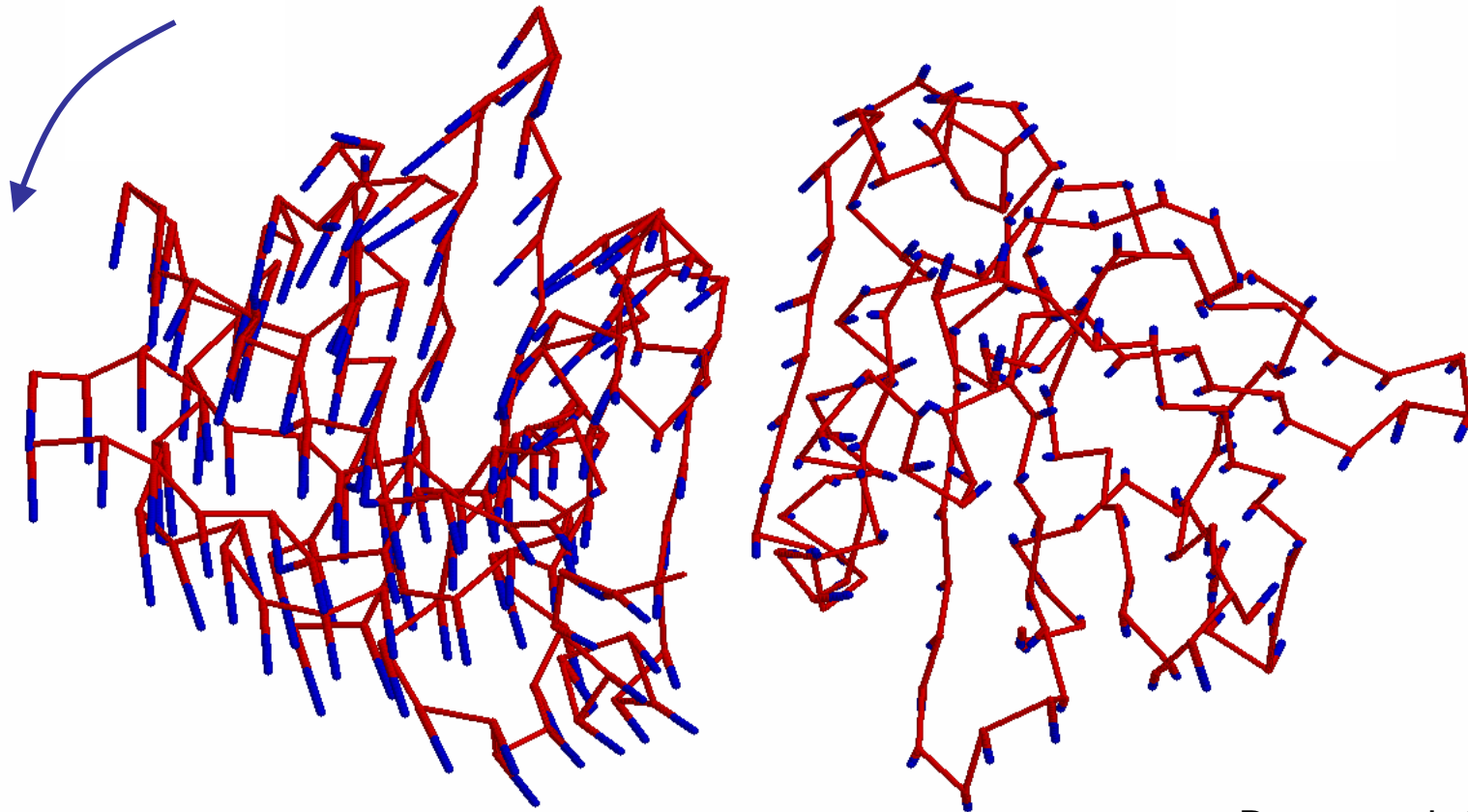
Number of H<sub>2</sub>O molecules in the protein



Baars et al. (2006)

## Results

Change of conformation / relative movement of monomers (650 MPa)



Baars et al. (2006)



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